# Phase Equilibrium in the System *Ln*–Mn–O IV. *Ln*=Sm at 1100°C

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Phase equilibrium in a Sm–Mn–O system has been established at 1100°C while changing the oxygen partial pressure from 0 to 13.00 in  $-\log (P_{O_2}/\text{atm})$ , and a phase diagram at 1100°C is presented for a Sm<sub>2</sub>O<sub>3</sub>–MnO–MnO<sub>2</sub> system. Under the experimental conditions, Sm<sub>2</sub>O<sub>3</sub>, MnO, Mn<sub>3</sub>O<sub>4</sub>, SmMnO<sub>3</sub>, and SmMn<sub>2</sub>O<sub>5</sub> phases are present at 1100°C, but Sm<sub>2</sub>MnO<sub>4</sub>, Mn<sub>2</sub>O<sub>3</sub>, and MnO<sub>2</sub> are unstable in the system. *Ln*Mn<sub>2</sub>O<sub>5</sub>- type phase is stable under the present experimental conditions differing from the previously reported La–Mn–O and Nd–Mn– O systems.

A wide range of nonstoichiometry has been found in the SmMnO<sub>3</sub> phase which coexisted with Sm<sub>2</sub>O<sub>3</sub>. X ranges from -0.010 at log  $P_{O_2} = -10.00$  to 0.098 at log  $P_{O_2} = 0$  in the molecular formula of SmMnO<sub>3+X</sub>. The nonstoichiometry is represented by an equation,  $N_O/N_{SmMnO_3} = 3.00 \times 10^{-4} (\log P_{O_2})^3 + 6.20 \times 10^{-3} (\log P_{O_2})^2 + 4.28 \times 10^{-2} (\log P_{O_2}) + 0.0979$ , and the activities of the components in the solid solution are calculated using the equation. SmMnO<sub>3</sub> seems to vary in composition in the Sm<sub>2</sub>O<sub>3</sub>-rich or Sm<sub>2</sub>O<sub>3</sub>-poor side as it was with LaMnO<sub>3</sub>. SmMn<sub>2</sub>O<sub>5</sub> is slightly nonstoichiometric.

Lattice constants of SmMnO<sub>3</sub> made under different oxygen partial pressures and those of SmMn<sub>2</sub>O<sub>5</sub> prepared in air were determined, along with spacings and relative intensities of SmMn<sub>2</sub>O<sub>5</sub>. Standard Gibbs energies of reactions shown in the system were calculated and compared with previously reported values.  $\odot$  2002 Elsevier Science (USA)

Key Words: phase equilibrium; thermogravimetry; Samariummanganese oxide; Standard Gibbs energy change of reaction.

#### **INTRODUCTION**

Many reports have been published on  $LaMnO_3$  from the view of magnetic, electronic, and crystallographic properties (1–3).

Kamata *et al.* (4) reported that the perovskite phase LaMnO<sub>3- $\lambda$ </sub> was revealed to have nonstoichiometry ranging from 2.947 to 3.079 under the oxygen partial pressure

below log  $(P_{O_2}/\text{atm}) = 0$  at 1200°C, and Nakamura *et al.* (5) reported that the stability limit of the perovskite phases expressed in terms of  $-\log (P_{O_2}/\text{bar})$  for LaMnO<sub>3</sub> is 15.05. Solid-state equilibrium relations were studied in the region of the La–Mn–O system bounded by LaMnO<sub>3</sub>, MnO, and La<sub>2</sub>O<sub>3</sub>, and in the temperature range 900–1380°C the defective perovskite LaMnO<sub>3- $\lambda}$ </sub> coexist directly in equilibrium with lanthanum oxide and manganous oxide (6). Van Roosmalen *et al.* (7) presented the pseudobinary La<sub>2</sub>O<sub>3</sub>–Mn<sub>2</sub>O<sub>3</sub> phase diagram in air and concluded that the perovskite-type LaMnO<sub>3+ $\lambda}$ </sub> solid solution can be formed with excess La as well as with excess Mn.

Recently, phase equilibria in the Ln-Mn-O (Ln = La (8), Nd (9), and Gd (10)) systems have been established at 1100°C. It has been found that not only LnMnO<sub>3</sub> type was stable in La-Mn-O and Nd-Mn-O systems as the ternary compound under the experimental conditions, but GdMn<sub>2</sub>O<sub>5</sub> was also stable in addition to GdMnO<sub>3</sub> in Gd-Mn-O system under the same experimental conditions. By this time, two types of phase diagram in Ln-Mn-O system have been found at 1100°C. That is: (1) only LnMnO<sub>3</sub> is present as the ternary compound and (2) LnMnO<sub>3</sub> and LnMn<sub>2</sub>O<sub>5</sub> compounds are present as the ternary compound.

LnMn<sub>2</sub>O<sub>5</sub>-type phase has already been reported to be stable in the Ln-Mn-O system. A compound LnMn<sub>2</sub>O<sub>5</sub> crystallize in the orthorhombic, Pbam (11). Decomposition temperatures of  $LnMn_2O_5$  (Ln = Pr, Nd, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb, and Y) were measured by thermogravimetry and differential thermal analysis under various oxygen partial pressures and the decomposition reactions were confirmed by identifying the decomposition products (12). By neutron diffraction method, the magnetic ordering of the rare-earth moments are studied at low temperatures in  $TMn_2O_5$  (T = Nd, Tb, Er) and the results were discussed on the basis of a polarization of the rare earths by the molecular field due to the manganese spins (13). RMn<sub>2</sub>O<sub>5</sub> (R=La, Pr, Nd, Sm, Eu, Tb, Ho, Er) have been prepared in polycrystalline form by a citrate technique, and excepting the Sm and Eu phases, structu-



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rally studied by high-resolution neutron powder diffraction. All the materials are isostructural (space group *Pbam*, Z = 4) and the magnetic properties strongly depend on the nature of R (14). The magnetoelectric effect of rare-earth oxides  $RMn_2O_5$  has been studied by a quasistatic magnetoelectric method for the purpose of determining whether linear magnetoelectric effect was present or not (15).

As is well known, in the Mn–O system there are four stable oxide-phases, MnO, Mn<sub>3</sub>O<sub>4</sub>, Mn<sub>2</sub>O<sub>3</sub>, and MnO<sub>2</sub>. However, only two-oxide phases, MnO and Mn<sub>3</sub>O<sub>4</sub>, are stable under the present experimental conditions (8–10), and the oxygen partial pressure in equilibrium with MnO and Mn<sub>3</sub>O<sub>4</sub> has been found to be -5.40 in log ( $P_{O_2}(\text{atm})$ ) (8).

In the Sm–Mn–O system,  $SmMnO_3$  and  $SmMn_2O_5$  ternary phases are stable. But the phase equilibrium in the Sm–Mn–O system has not been established even at high temperatures.

In consideration of the above circumstances, the objectives of the present study are: (1) to establish a detailed phase diagram of the Sm–Mn–O system at 1100°C as a function of the oxygen partial pressure and to ascertain the nonstoichiometric range of SmMnO<sub>3</sub> and SmMn<sub>2</sub>O<sub>5</sub>, (2) to determine the thermochemical properties based on the established phase diagram, and (3) to obtain the crystallographic data of SmMn<sub>2</sub>O<sub>5</sub> if it would be stable under the present experimental conditions.

#### **EXPERIMENTAL**

Analytical-grade  $Sm_2O_3$  (99.9%) and MnO (99.9%) were used as starting materials. MnO was dried by heating at 110°C in air, and  $Sm_2O_3$  was dried at 1100°C. Mixtures with desired ratios of  $Sm_2O_3/MnO$  were prepared by mixing in an agate mortar with repeated intermittent calcination by solid reaction at 1100°C. This procedure is the same as that described previously (16).

Mixed gases of  $CO_2$  and  $H_2$ , and  $CO_2$  and  $O_2$ , and single-component gases of  $O_2$  and  $CO_2$  were used to obtain the oxygen partial pressures in the present experiment.

The apparatus and procedures for controlling the oxygen partial pressure, maintaining constant temperature, the method of thermogravimetry, and the criterion for the establishment of equilibrium were the same as those described in the previous paper (16). Briefly, to ensure equilibrium, the equilibrated point of each sample at a given oxygen partial pressure was determined from both sides of the reaction, that is, from low oxygen partial pressures to high oxygen partial pressures, and vice versa. The oxygen partial pressure in equilibrium was determined as follows. As is known from the Gibbs phase rule, the freedom in a three-phrase regions is zero under present experimental conditions. That is, the oxygen partial pressure in equilibrium is invariable and defined by the experimental temperature and pressure conditions. For example, for  $0.60 \text{Sm}_2\text{O}_3/0.40 \text{MnO}$  (Fig. 1a),  $\log P_{\text{O}_2} =$ 10.00 is invariable under given temperature and pressure conditions. The exact value is obtained through experiment: to determine the oxygen partial pressure in equilibrium, the weight of sample on a balance is measured while the sample is taken through the three phase regions by controlling the  $\text{CO}_2/\text{H}_2$  ratio. If the stabilized oxygen partial pressure is higher than the oxygen partial pressure in equilibrium, the sample on the balance will become heavier, and vice versa. Repeating the procedure, the oxygen partial pressure will approach that in equilibrium.

Schematics of the balance, furnace, and gas mixer are given in the previous report (17). The furnace is installed vertically and employs as its heating element a mullite tube wound with Pt 60%–Rh 40% alloy wire. Mixed gases pass from the bottom of the furnace to the top.

The identification of phases and the determination of lattice constants were performed using an X-ray diffractometer (Rint 2500, Rigaku) with Ni-filtered CuK $\alpha$  radiation. A specimen of silicon was used to calibrate  $2\theta$  as an external standard.

## **RESULTS AND DISCUSSIONS**

# $Sm_2O_3$ -MnO- $MnO_2$ system

The Mn–O system at 1100°C related to the present phase diagram has been described in previous works (8, 9). Here, the results are briefly described as follows; the MnO and Mn<sub>3</sub>O<sub>4</sub> phases are stable, and MnO is nonstoichiometric, whereas Mn<sub>3</sub>O<sub>4</sub> is stoichiometric. The oxygen partial pressure in equilibrium with MnO and Mn<sub>3</sub>O<sub>4</sub> is -5.40 in log ( $P_{O_2}(\text{atm})$ ).

Six samples, having  $Sm_2O_3/MnO$  mole ratios of 0.6/0.4, 0.4/0.6, 0.3/0.7, 0.25/0.75, 0.15/0.85, and 0.1/0.9, were prepared for thermogravimetry. Figure 1 shows the oxygen partial pressure  $-\log(P_{O_2}(atm))$ , versus the weight changes,  $W_{\rm O_2}/W_{\rm T}$ , for three representative samples: 0.6/ 0.4 (Fig. 1a), 0.25/0.75 (Fig. 1b), and 0.15/0.85 (Fig. 1c). Here,  $W_{O_2}$  is the weight increase of a sample from the reference weight at  $\log (P_{O_2}(atm)) = -13.00$ , at which  $Sm_2O_3$  and MnO are stable, and  $W_T$  is the total weight gain from reference state to the state at 1 atm  $O_2$ , at which Sm<sub>2</sub>O<sub>3</sub> and SmMnO<sub>3</sub>, or SmMnO<sub>3</sub> and SmMn<sub>2</sub>O<sub>5</sub> or  $SmMn_2O_5$  and  $Mn_3O_4$  are stable, depending on the overall composition of the samples. As is evident from Fig. 1, weight breaks are found at 10.00, 5.40, and 1.55 in  $-\log(P_{\Omega_2}(\text{atm}))$ . These values correspond to the oxygen partial pressure in equilibrium with the three solid phases,  $Sm_2O_3 + SmMnO_3 + MnO$ ,  $SmMnO_3 + MnO + Mn_3O_4$ , or  $SmMnO_3 + Mn_3O_4 + SmMn_2O_5$ , respectively.

Table 1 shows the results of identified phases in the Sm-Mn-O system, together with the experimental



FIG. 1. Relationships between the oxygen partial pressure, log ( $P_{O_2}(atm)$ ), and the weight change of the samples,  $W_{O_2}/W_T$ . (a) Sm<sub>2</sub>O<sub>3</sub>/MnO = 0.60/ 0.40, (b) Sm<sub>2</sub>O<sub>3</sub>/MnO = 0.25/0.75, and (c) Sm<sub>2</sub>O<sub>3</sub>/MnO = 0.15/0.85.

Identification of Phase						
Sample (mol ratio)						
Sm <sub>2</sub> O <sub>3</sub>	MnO	$-\log(P_{O_2}(atm))$	Time (h)	Phase		
0.6	0.4	13.00	8	Sm <sub>2</sub> O <sub>3</sub> +MnO		
		10.50	8	$Sm_2O_3 + MnO$		
		9.00	13	$Sm_2O_3 + SmMnO_3$		
		0.68	14.5	$Sm_2O_3 + SmMnO_3$		
0.4	0.6	13.00	8	Sm <sub>2</sub> O <sub>3</sub> +MnO		
		10.50	8	$Sm_2O_3 + MnO$		
		9.00	13	$Sm_2O_3 + SmMnO_3$		
		0.68	14.5	$Sm_2O_3 + SmMnO_3$		
0.25	0.75	13.00	8	$Sm_2O_3 + MnO$		
		10.50	8	$Sm_2O_3 + MnO$		
		9.00	13	$SmMnO_3 + MnO$		
		6.00	16	$SmMnO_3 + MnO$		
		5.00	18.5	$SmMnO_3 + Mn_3O_4$		
		2.00	19.5	$SmMnO_3 + Mn_3O_4$		
		0.68	120	$SmMnO_3 + SmM$ -		
				$n_2O_5$		
0.1	0.9	13.00	8	$Sm_2O_3 + MnO$		
		10.50	8	$Sm_2O_3 + MnO$		
		9.00	13	$SmMnO_3 + MnO$		
		6.00	16	$SmMnO_3 + MnO$		
		5.00	18.5	$SmMn_2O_5 + Mn_3O_4$		
		2.00	19.5	$SmMn_2O_3 + Mn_3O_4$		
		0.68	120	$SmMn_2O_5 + Mn_3O_4$		
0.0	1.0	13.00	6	MnO		
		5.00	46.5	$Mn_3O_4$		
		0.68	46.5	$Mn_3O_4$		

TABLE 1 Identification of Phase

conditions. Samples of about 500 mg were prepared for the identification of phases by means of the quenching method. Five phases,  $Sm_2O_3$ , MnO,  $Mn_3O_4$ ,  $SmMnO_3$ , and  $SmMn_2O_5$  were found to be stable by X-ray diffractometer and were found to be stable under the experimental conditions.

From the above results of thermogravimetry and phase identification, a phase diagram was drawn and shown in Fig. 2 as a  $\text{Sm}_2\text{O}_3$ -MnO-MnO<sub>2</sub> system, although MnO<sub>2</sub> is not stable under the experimental conditions. The numerical values in the three solid fields in Fig. 2 are the values of  $-\log P_{\text{O}_2}$  in equilibrium with the three solid phases described above, and those found in the two-phase regions are also the oxygen partial pressures in  $\log P_{\text{O}_2}$ , which are shown by dotted lines. Nonstoichiometry of MnO is ascertained by the results of thermogravimetry of the other two samples, shown in Figs. 1b and 1c. That is, nonstoichiometry is represented by slight changes in the composition in the range from 10.00 to 5.40 in  $-\log P_{\text{O}_2}$ .

SmMnO<sub>3</sub> has a large nonstoichiometric composition within the range from -10.00 to 0 in log  $P_{O_2}$ . Fig. 3 shows the relationship between the oxygen partial pressure and the composition of the SmMnO<sub>3</sub> solid solution, which coexisted with Sm<sub>2</sub>O<sub>3</sub>. This curve is represented by an equation:  $N_{\rm O}/N_{\rm SmMnO_3} = 3.00 \times 10^{-4} (\log P_{\rm O_2})^3 + 6.20 \times 10^{-3} (\log P_{\rm O_2})^2 + 4.28 \times (\log P_{\rm O_2}) + 0.0979$ . Here, N<sub>O</sub> and  $N_{\rm SmMnO_3}$  represent the mole fraction of oxygen and  $SmMnO_3$  in the solid solution. This equation can be solved to show that samarium-manganese perovskite would be stoichiometric at -7.00 in log ( $P_{O_2}(atm)$ ). As shown in Fig. 2, the composition of the SmMnO<sub>3</sub> solid solutions on the Sm<sub>2</sub>O<sub>3</sub>-rich side and that on Sm<sub>2</sub>O<sub>3</sub>-poor side are not the same. This suggested that the region exhibits some width with respect to the direction between the  $Sm_2O_3$  side and the  $Mn_3O_4$ . Van Roosmalen *et al.* (7) reported that a perovskite-type  $LaMnO_{3+\delta}$  solid solution can be formed with excess La as well as with excess Mn. The same phenomenon was also found in the other Ln-Mn-O systems (8–10). However, its width has not been detected by the present experimental techniques. The curved line of  $\log P_{O_2}$  might be drawn from Gibb's phase rule, that is, one-phase region, SmMnO<sub>3</sub>, of a three-component system has two degrees of freedom. Consequently, the oxygen partial pressure lines in one-phase area could be curved if its phase would be area.



FIG. 2. Phase equilibrium in the  $\text{Sm}_2\text{O}_3$ -MnO-MnO<sub>2</sub> system at 1100°C. Numerical values in the three-phase regions are the oxygen partial pressures in  $-\log(P_{\text{O}_2}(\text{atm}))$  in equilibrium with three solid phases, which are shown in the regions. Dotted lines in two-phase regions are also the oxygen partial pressures indicated by the lines. Abbreviations are the same as those used in Table 2.



FIG. 3. Oxygen partial pressure,  $-\log(P_{O_2}(atm))$  versus the composition of SmMnO<sub>3</sub> solid solution,  $N_O/N_{SmMnO_3}$ .

Compositions, symbols, stability ranges in oxygen partial pressures of compounds and activities of components in the solid solutions are tabulated in Table 2.

Lattice constants of SmMnO<sub>3</sub> perovskite were determined as orthorhombic at 9.00, 5.00, and 0.68 in  $-\log P_{O_2}$ from samples of Sm<sub>2</sub>O<sub>3</sub>/MnO at mole ratios of 0.4/0.6 and 0.25/0.75. These samples were selected for their ability to coexist with Sm<sub>2</sub>O<sub>3</sub> or Mn<sub>3</sub>O<sub>4</sub>. The results are tabulated in Table 3 together with the previously reported values. Slight differences were found in the lattice constants and the volume among Sm<sub>2</sub>O<sub>3</sub> coexisted samples, depending on the oxygen partial pressure. The samples prepared in 0.68 in  $-\log P_{O_2}$  are of smaller volume than those prepared at 9.00 in  $-\log P_{O_2}$ . This could stem from the difference in the ionic radii of Mn<sup>3+</sup> 0.72 Å and Mn<sup>4+</sup> 0.68 Å, with each having a coordination number 6, respectively (21). The content of Mn<sup>4+</sup> in the solid solution prepared in

 
 TABLE 2

 Compositions, Stability Ranges in Oxygen Partial Pressures, and Activities of Components in Solid Solutions

Component	Compositions	$-\log(P_{O_2}(atm))$	$\log a$	Symbol
MnO	MnO <sub>1.000</sub>	13.00-10.00	0	<b>B</b> <sub>1</sub>
	$MnO_{1.02}$	5.40	$-9.58 \times 10^{-3}$	$B_2$
SmMnO <sub>3</sub>	SmMnO <sub>2.997</sub>	10.00	0	$W_1$
	SmMnO <sub>3.012</sub>	5.40	$-5.31 \times 10^{-3}$	W <sub>2</sub>
	SmMnO <sub>3.039</sub>	1.55	$-2.40  imes 10^{-2}$	W <sub>3</sub>
SmMn <sub>2</sub> O <sub>5</sub>	$SmMn_2O_{4.92}$	1.55	0	$D_1$
	$SmMn_2O_5$	0.00	$-1.13\times10^{-2}$	$D_2$

Note.  $(N_{\rm O}/N_{\rm SmMnO_3}) = 0.0003(\log P_{\rm O_2})^3 + 0.0062(\log P_{\rm O_2})^2 + 0.0428(\log P_{\rm O_2}) + 0.0979$ 

 $(N_{\rm O}/N_{\rm SmMn_2O_5}) = -0.0156(\log P_{\rm O_2})^2 + 0.0291(\log P_{\rm O_2}) + 0.0011.$ 

 $\log P_{O_2} = -0.68$  must be more than that prepared in  $\log P_{O_2} = -9.00$  resulting from Fig. 2.

# Compound, $SmMn_2O_5$

In the Sm–Mn–O system  $\text{SmMn}_2\text{O}_5$  is stable as a ternary compound unlike the La and Nd systems. Preparing the compound by means of the usual solid-state reaction is very difficult, on account of the slow reaction rate. It takes more than 3 days in air to prepare  $\text{SmMn}_2\text{O}_5$  by heating a mixture of  $\text{Sm}_2\text{O}_3$  and MnO at even  $1100^{\circ}\text{C}$ .

The compound have nonstoichiometric composition, and the relationship between the oxygen partial pressure and the composition of  $\text{SmMn}_2\text{O}_5$  solid solution,  $N_O/N_{\text{SmMn}_2\text{O}_5}$ , is shown with an equation,  $N_O/N_{\text{SmMn}_2\text{O}_5} =$  $-0.0156(\log P_{\text{O}_2})^2 + 0.0291(\log P_{\text{O}_2}) + 0.0011$ . Lattice constants and spacings were determined based upon the data of NdMn<sub>2</sub>O<sub>5</sub> (22) because the ionic radius of Nd is close to that of Sm. Results of lattice constant are shown in Table 4 together with previously reported values. The determined spacings and relative intensities are also shown in Table 5. Observed d(obs.) values are in good agreement with calculated d(cal.) values.

# Standard Gibbs Energy Change of Reaction

On the basis of the established phase diagram, the standard Gibbs energy changes of reactions in Table 4 were determined by the equation,  $\Delta G^{\circ} = -RT \ln K$ . Here *R* is the gas constant, *T* the absolute temperature, and *K* the equilibrium constant of the reaction. The standard state of the activities of components in the solid solutions can be

Sample (mol	ratio)							
Sm <sub>2</sub> O <sub>3</sub>	MnO	$-\log(P_{O_2}(atm))$	Time (h)	a (Å)	b (Å)	c (Å)	V (Å) <sup>3</sup>	Coexistent phase
0.4	0.6	9.0	13	5.363 (5)	5.842 (5)	7.481 (9)	234.4 (4)	Sm <sub>2</sub> O <sub>3</sub>
		5.0	23.5	5.362 (4)	5.843 (4)	7.474 (6)	234.2 (3)	$Sm_2O_3$
		0.68	14.5	5.365 (6)	5.796 (5)	7.493 (9)	233.0 (4)	$Sm_2O_3$
0.25	0.75	9.0	13	5.358 (3)	5.849 (3)	7.474 (4)	234.2 (2)	MnO
		5.0	18.5	5.350 (3)	5.802 (3)	7.481 (3)	232.2 (2)	$Mn_3O_4$
		0.68	120	5.353 (5)	5.796 (7)	7.847 (10)	232.3 (5)	SmMn <sub>2</sub> O <sub>5</sub>
Ref. (18)		_	_	5.358	5.825	7.483	_	_
Ref. (19)		_	_	5.376	5.788	7.520	_	_
Ref. (20)		—	—	5.357	5.825	7.482	—	_

TABLE 3Lattice Constants of Quenched SmMnO3

arbitrarily chosen for each solid solution and is indicated as  $\log a_i = 0$  in Table 2.

Calculated values for reactions which appear in the phase diagram is shown in Table 6. The  $\Delta G^{\circ}$  value for reaction (1) is -65.6 kJ/mol. This value is larger than those of -85.3 for LaMnO<sub>3</sub>, and -71.3 for NdMnO<sub>3</sub>, and is smaller than -62.2 for GdMnO<sub>3</sub> as expected from the oxygen partial pressure in equilibrium.

For reaction (2), the oxygen partial pressure in equilibrium is -1.55 in  $\log (P_{O_2}/\text{atm})$  and  $\Delta G^{\circ} = 13.7 \text{ kJ}/\text{mol}$ . As is shown in Fig. 2, SmMn<sub>2</sub>O<sub>5</sub> is nonstoichiometric. Therefore, taking the activity of component of SmMn<sub>2</sub>O<sub>5</sub> at the composition  $D_1$  to be unity, the  $\Delta G^{\circ}$  value was calculated. Satoh *et al.* (12) reported the oxygen partial pressure -1.54 in  $\log P_{O_2}$  for the reaction by means of emf measurement of solid electrolyte. The present value, 1.55, is in good agreement with the previously reported value.

The previously reported values of  $\Delta G^{\circ}$  and the oxygen partial pressure in equilibrium with MnO and Mn<sub>3</sub>O<sub>4</sub> are quoted from Ref. (23–25). The standard Gibbs energy change for reaction (3) is  $-72.1\pm0.3$  kJ/mol. Taking the activity of MnO of the composition (B<sub>2</sub>) to be unity,  $-75.0\pm0.3$  kJ/mol was obtained. In spite of the small solid solution range, this difference is larger than the experimental error. -73.9, -50.9, and -60.4 kJ/mol are obtained from the previous data of (23), (24) and (25), respectively. Our value is in good agreement with Hahn *et al.* (23)

# The Relationship between the Ionic Radius of Lanthanoid and $\Delta G^{\circ}$ Value

The reaction,  $\frac{1}{2}Ln_2O_3 + MnO + \frac{1}{4}O_2 = LnMnO_3$ , is common in the *Ln*-Mn-O system. The  $\Delta G^{\circ}$  values for the reactions versus the ionic radius of lanthanoid elements with 12 coordination in the perovskite structure (26) is shown in Fig. 4. In Fig. 4 the present value is shown together with the previous values which were presented by one of us. Although only four data have been obtained so far, the figure indicates a linear relation between  $\Delta G^{\circ}$  and the ionic radius. The same phenomenon at 1273 K was found by Atsumi *et al.* (27).

### CONCLUSIONS

(1) A phase equilibrium in the system Sm–Mn–O at  $1100^{\circ}$ C was established under an oxygen partial pressure from 0 to -13.00 in log ( $P_{O_2}(atm)$ ).

(2) Under the present experimental conditions, the  $Sm_2O_3$ , MnO, Mn<sub>3</sub>O<sub>4</sub>, SmMnO<sub>3</sub> and SmMn<sub>2</sub>O<sub>5</sub> phases are stable.

 TABLE 4

 Lattice Constant of Quenched SmMn<sub>2</sub>O<sub>5</sub>

Sample (mol rat	tio)					
Sm <sub>2</sub> O <sub>3</sub>	MnO	Time (h)	<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	V (Å)
0.2	0.8	95.5	7.448 (5)	8.579 (3)	5.686 (2)	363.3 (3)
Ref. (12)		_	7.445 (6)	8.585 (7)	5.68 (4)	363
Ref. (14)		—	7.4332 (7)	8.5972 (7)	5.6956 (5)	363.55 (9)

Note. SmMn<sub>2</sub>O<sub>5</sub> was prepared at  $1100^{\circ}$ C in  $-\log(P_{O_2}(\text{atm})) = 0.68$ .

TABLE 5

h	k	l	<i>d</i> (obs.)	d (calc.)	$I/I_0 \times 100$
0	0	1	5.72	5.69	22
0	2	0	4.30	4.29	2
1	1	1	4.008	3.999	2
1	2	0	3.725	3.717	19
1	2	1	3.117	3.111	76
2	1	1	2.930	2.928	100
2	2	0	2.814	2.812	8
1	3	0	2.673	2.670	39
1	1	2	2.542	2.537	25
1	3	1	2.420	2.417	4
0	2	2	2.375	2.370	15
1	2	2	2.262	2.258	11
2	1	2	2.187	2.185	26
1	4	0	2.063	2.061	13
0	4	1	2.009	2.007	15
0	0	3	1.897	1.895	3
3	3	0	1.874	1.875	5
2	4	1	1.767	1.767	5
0	4	2	1.714	1.712	12
2	0	3	1.691	1.689	10
1	4	2	1.670	1.669	5
1	5	1	1.605	1.604	2
4	3	0	1.565	1.560	18
4	1	2	1.531	1.533	3
2	5	1	1.503	1.503	10
3	1	3	1.486	1.484	1
4	2	2	1.465	1.464	2
1	5	2	1.442	1.441	6
0	0	4	1.423	1.422	11
0	1	4	1.405	1.402	5
1	4	3	1.396	1.395	4
0	6	1	1.388	1.387	2
3	3	3	1.333	1.333	4
0	6	2	1.278	1.277	1
3	5	2	1.269	1.264	1
1	3	4	1.256	1.255	7
3	1	4	1.222	1.221	3
2	5	3	1.204	1.204	4

(3) MnO, SmMnO<sub>3</sub>, and SmMn<sub>2</sub>O<sub>5</sub> have nonstoichiometric composition. However, Mn<sub>3</sub>O<sub>4</sub> is stoichiometric.

TABLE 6 Standard Gibbs Energy Changes of Reaction at 1100°C

Reaction	$-\log P_{O_2}(atm)$	$-\Delta G^{\circ}(\mathrm{kJ/mol})$
(1) MnO + $\frac{1}{2}$ Sm <sub>2</sub> O <sub>3</sub> + $\frac{1}{4}$ O <sub>2</sub> $\rightarrow$ SmMnO <sub>3</sub>	10.00	65.6
(2) SmMn $\tilde{O}_3 + \frac{1}{3}Mn_2\tilde{O}_4 + \frac{1}{3}O_2 \rightarrow SmMn_2O_5$	1.55	14.2
(3) $3MnO + \frac{1}{2}O_2 \rightarrow Mn_3O_4$	5.40	72.1
-	5.62	$73.9^{a}$
	(3.87)	$50.9^{b}$
	(4.60)	60.4 <sup>c</sup>

<sup>a</sup> Ref. (23).

<sup>c</sup> Ref. (25).



FIG. 4. The ionic radius of lanthanoid element in 12 coordination number versus  $\Delta G^{\circ}$  value of the reaction,  $\frac{1}{2}Ln_2O_3 + MnO + \frac{1}{4}O_2 = LnMnO_3$ .

(4) Standard Gibbs energies of reactions found in the diagram were calculated with the oxygen partial pressure in equilibrium with three solid phases.

(5) Lattice constants of SmMnO<sub>3</sub> and SmMn<sub>2</sub>O<sub>5</sub>, and spacings and relative intensities of SmMn<sub>2</sub>O<sub>5</sub> were determined.

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#### REFERENCES

- 1. J. B. Goodenough, Prog. Solid State Chem. 5, 149 (1971).
- 2. C. N. R. Rao, Annu. Rev. Phys. Chem. 40, 291 (1989).
- 3. B. C. Tofield and W. R. Scott, J. Solid State Chem. 10, 183 (1974).
- 4. K. Kamata, T. Nakajima, T. Hayashi, and T. Nakamura, Mater. Res. Bull. 13, 49 (1978).
- 5. T. Nakamura, G. Petzow, and L. J. Gauckler, Mater. Res. Bull. 14, 649 (1979).
- 6. M. Lucco Borlera and F. Abbattista, J. Less-Common Met. 92, 55 (1983).
- 7. J. A. M. Van Roosmalen, P. Van Vlaanderen, E. H. P. Cordfunke, W. L. Ijdo, and D. J. W. Ijdo, J. Solid State Chem. 114, 516 (1995).
- 8. K. Kitayama, J. Solid State Chem. 153, 336 (2000).
- 9. K. Kitayama and T. Kanzaki, J. Solid State Chem. 158, 236 (2001).
- 10. K. Kitayama, H. Ohno, R. Ide, K. Satoh, and S. Murakami, J. Solid State Chem., submitted.
- 11. S, Quezel-Ambrunaz, F. Bertaut, and G. Buisson, C. R. Acad. Sci. Paris 258, 3025 (1964).
- 12. H. Satoh, S. Suzuki, K. Yamamoto, and N. Kamegashira, J. Alloys Compd. 234, 1 (1996).
- 13. G. Buisson, Phys. Stat. Sol. 17, 191 (1973).

Spacing and relative intensities

<sup>&</sup>lt;sup>b</sup> Ref. (24).

- J. A. Alonso, M. T. Casais, M. J. Martinez-Lope, J. L. Martinez, and M. T. Fernandez-Diaz, J. Phys.: Condens. Matter 9, 8515 (1997).
- 15. H. Nakamura and K. Kohn, Ferroelectrics 204, 107 (1997).
- K. Kitayama, K. Nojiri, T. Sugihara, and T. Katsura, J. Solid State Chem. 56, 1 (1985).
- 17. K. Kitayama, J. Solid State Chem. 137, 255 (1998).
- 18. JCPDS Card No. 25-747.
- A. Waintal, J. J. Capponi, E. F. Bertaut, M. Contre, and D. Francois, Solid State Commun. 4, 125 (1966).
- T. Arakawa, A. Yoshida, and J. Shiokawa, *Mater. Res. Bull.* 15, 269 (1980).
- 21. R. D. Shannon and C. T. Prewitt, Acta Crystallogr. B 25, 925 (1965).

- 22. JCPDS Card No. 79-1691.
- 23. W. C. Hahn, Jr. and A. Muan, Am. J. Sci. 258, 66 (1960).
- J. F. Elliott and M. Gleiser, "Thermochemistry for Steelmaking," Vol. 1. Addison–Wesley, Reading, MA, 1960.
- 25. R. A. Robie, R. S. Hemingway, and J. R. Fisher, "Thermodynamic Properties of Minerals and Related Substances at 298.15 K and 1 Bar (10<sup>5</sup> Pascals) Pressure and at Higher Temperatures." Geological Survey Bulletin 1452. United States Government Printing Office, Washington, 1978.
- 26. G. P. Espinosa, J. Chem. Phys. 37, 2344 (1962).
- 27. T. Atsumi, T. Ohgushi, and N. Kamegashira, J. Alloys Compd. 238, 35 (1996).